

VINAYAKA MISSION'S RESEARCH FOUNDATIONS, SALEM
(Deemed to be University)

Pharm.D DEGREE EXAMINATION - July 2019

First Year

REMEDIAL MATHEMATICS

Time: Three hours

Maximum: 70 marks

I. Write essays on any **TWO** questions: (2 x 15 = 30)

1. Show that
$$\begin{vmatrix} 1 & a^2 & a^3 \\ 1 & b^2 & b^3 \\ 1 & c^2 & c^3 \end{vmatrix} = (a-b)(b-c)(c-a)(ab+bc+ca)$$

2. Evaluate
$$\int_0^1 \frac{x^2}{1+x^2} dx$$

3. Prove $a^2=b^2+c^2-2bc \cos A$ for any triangle ABC

II. Write short answers on any **SIX** questions: (6 x 5 = 30)

4. If $x^y = e^{x-y}$ then show that
$$\frac{dy}{dx} = \frac{\log x}{(1+\log x)^2}$$

5. Differentiate $y = x^x$ with respect to x

6. Solve: $\sqrt{1+x^2} dx + \sqrt{1+y^2} dy = 0$

7. If $A = \begin{pmatrix} 3 & -1 & 2 \\ 1 & 2 & 2 \\ 2 & 0 & 5 \end{pmatrix}$ then find A^2

8. If $A = \begin{pmatrix} -1 & 2 \\ 2 & 4 \end{pmatrix}$ $B = \begin{pmatrix} 3 & 5 \\ 6 & -7 \end{pmatrix}$ then show that $(AB)' = B'A'$

9. Derive the standard equation of a parabola $y^2=4ax$.

10. A circle passes through (2, -3) and its centre is (4,4). Find its equation.

11. Find $L\{e^{2t} t^2\}$.

III. Write short notes on any **FIVE** question: (5 x 2 = 10)

12. Find the trace of the matrix
$$\begin{pmatrix} 1 & 3 & -5 \\ 2 & -1 & 5 \\ 2 & 0 & 1 \end{pmatrix}$$

13. Find the equation of straight line passing through (1,0) having slope -1

14. Evaluate :
$$\lim_{x \rightarrow \infty} \frac{x^2 + 5x + 2}{2x^2 - 5x + 1}$$

15. If $y = e^{x(x^4)}$ find $\frac{dy}{dx}$

16. If $A = \begin{pmatrix} 2 & 3 & 4 \end{pmatrix}$ $B = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$. Find the sum $A + B'$.

17. Find the midpoint of line joining (-3, -2) and (3, 2).